

Nexus: A Peer-to-Peer Network

July 4, 2017

Abstract

“You never change things by fighting the existing reality. To change something, build a new model that makes the existing model obsolete”

R. Buckminster Fuller

Throughout history we have witnessed many changes in our culture, technology, and governance. These changes are fueled by a necessity for the further evolution of mankind. Now humanity approaches another one of these times in history, where the way everything has been done must be changed; this is why we built Nexus. Peer-to-Peer technology fuels the backbone of a global blockchain-based cryptocurrency represented by the ticker: *NXS* which is traded world-wide as an alternative currency with the capacity to rival world economies. The framework, Nexus, utilizes new distributed database designs, mathematical trust, community governance, ground-based mesh networks, and a *Low Earth Orbit* Satellite Constellation. We are Nexus, a connection of people, ideas, and computers providing greater choice and therefore greater evolution with an aim towards our freedom. Welcome to the Future.

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“fides in stellis, virtus in numeris”



nexus: a connection or series of connections linking two or more things.

Oxford English Dictionary

1 Introduction

Peer-to-peer networks are forming the foundations of digital industries world-wide. This ecosystem continues to evolve as innovators advance the growing body of open-source protocols, including *Bitcoin*, *BitTorrent*, *TOR*, and *IPFS*. The utility of these networks has increasingly affected people throughout the world. For the first time in history, the transmission of value can occur without the need for intermediaries. Now, almost ten years from the release of Satoshi Nakamoto's *Bitcoin: A Peer-to-Peer Electronic Cash System* [1] debuted on a Cypher Punk e-mail list in a time of economic crisis, many benefits have been realized including but not limited to: *viz.* enhanced financial security, emancipation from centralized banking systems, and the possibilities of future applications of blockchains. However, many challenges have also been identified such as scaling, consensus updates, and considerations for the post-quantum era that is almost upon us. By resolving some of these identified issues, Nexus has enhanced the blockchain protocol, thereby providing a solid foundation for the digital economies of the future.

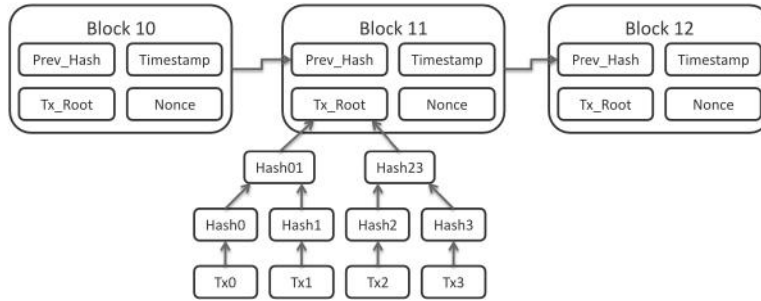
1.1 What is Nexus?

Nexus is a connection, or series of connections, of computers, businesses, and people with a focus on establishing new applications of finance, technology, service, and sovereignty.

1.2 What is a Blockchain?

A blockchain is a decentralized and immutable public database of transactions. The database is organized by connecting a chain of blocks together. Each block contains a group of transactions. The blocks are ordered in time

and "chained" together using cryptographic hashes.¹² Large quantities of computational resources must be expended to create each block hash,³ and each block contains the previous block's hash: *this is how they are chained*.



The blocks are produced in intervals, forming a chain of verifiable blocks that contain the transaction history providing data a form that cannot be altered without redoing the work of the *previous blocks* or *confirmations*. The end result is a single, immutable journal of transactions grouped through time-ordered blocks distributed and verified by all of the nodes on the network.

1.3 How are Blocks Created?

Blocks are created by a distributed network of miners (*users operating special hardware to solve the proof of work puzzles*) in a process called mining. As an analogy for mining, imagine many people are sitting in a room out of motivation to win a prize if they solve their Rubik's Cube first. The tiles of the Rubik's Cube can be thought of as the transactions, with one of these tiles representing the prize (*mint*) the winner is allowed to claim if they solve the cube. However, they are only allowed to make one random change per iteration and they are limited by the speed of their hands (*some may be faster than others*). Eventually one player will end up with a solved cube. When one finds the solution, they show it to the other players in the room. If the other players independently verify that the cube is solved properly, the winner is rewarded with the prize and a new round begins.

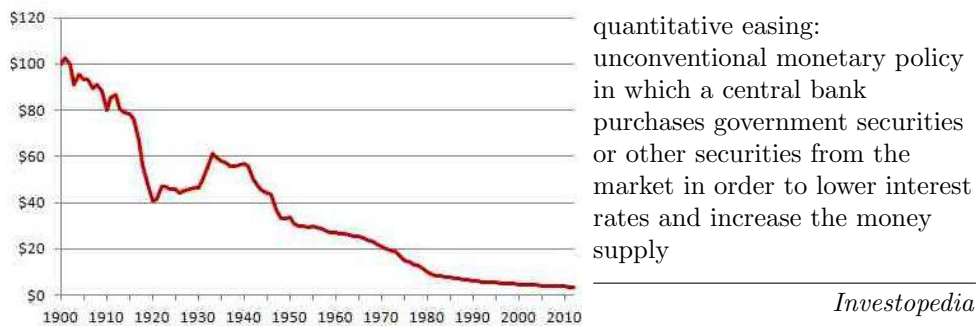
¹²A cryptographic hash function is a hash function which takes an input (or 'message') and returns a fixed-size alphanumeric string. The string is called the 'hash value'..." [10]

²The concept of a cryptographic chain of blocks dates back to Ehram, Meyer, Smith and Tuchman's invention of Cipher Block Chaining (CBC) in 1976 [3]. NB: this is distinct from *blockchain* as discussed here in many ways, notably because it does not include a proof-of-work.

³This is generically called Proof-of-Work but also includes Sunny King's innovation: Proof-of-Stake [11].

1.4 Are Blockchains the Answer?

Blockchains have become more necessary as we become aware of the challenges we are facing in our current progression as a society. By maintaining open minds to recognize the challenges we face, we become aware of the limitations that legacy monetary systems cannot solve. As is seen that *blockchains* do solve many monetary challenges, such as uncontrolled inflation, central banking, and many others, they are only a part of the solution to our current economic circumstances.



The term *blockchain* should not be confused with any encrypted database. The dollar is essentially an online virtual currency encrypted between banks that is redeemable for federal reserve notes *Paper Money*. This does not make the dollar a blockchain. What makes a blockchain is a decentralized public journal with no central authority. By owning a particular portion of a cryptocurrency, you prove partial ownership in the financial system.

1.5 Challenges of Money

The application and implementation of the world's monetary systems has become the source of one of the biggest challenges we face today. This is due to the many global policies designed for empowering central banks to create currencies as debt with interest associated. Central Banks have the ability to influence world economies by changing interest rates, printing massive sums of money (*otherwise known as inflation / hyperinflation*), quantitative easing, or through various other forms of credit creation. There are many historical examples of central authorities who have misused this enormous power, knowingly or unknowingly, to the detriment of the people that these institutions exist to serve. These include post-World War I Germany with a hyperinflation of up to 30,000% per month, Zimbabwe during the Great Recession of the last decade with nearly 79 billion percent per month

inflation, and post-World War II Hungary, with inflation rates of nearly *13,000,000,000,000%* per year. ⁴.

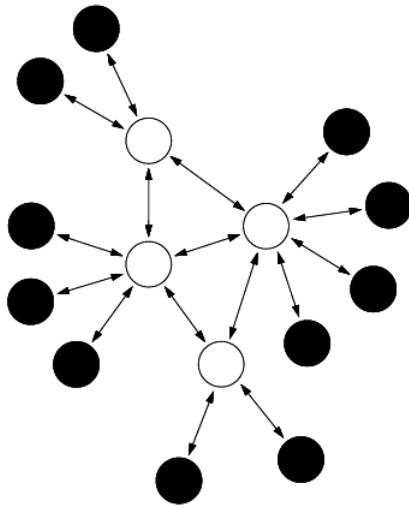
2 Nexus

Multiple components need to be considered when providing the fundamental basis for change and freedom. The following is a brief outline of the core components that comprise the foundation of Nexus.

2.1 Hardware

Nexus is researching and developing three types of networks that will work together to form a new telecommunications system. These are outlined in the sections below.

2.1.1 Mesh Networks



A mesh network is a network topology in which each node relays data for the network. All mesh nodes cooperate in the distribution of data in the network [4].

This allows for the growth of ground-based networks to handle data exchange in localized areas.

Ground-based mesh networks will solve many telecommunication issues. Specialized antennas can be produced for people to purchase and operate, thereby

forming networks owned by the individuals who built it.

2.1.2 Cube Satellites

As mesh networks grow, they will need to overcome the problem with line of sight and transcontinental communication. This issue can be solved with the deployment of a satellite constellation designed to focus towards orbital

⁴The estimated 200% per day inflation equates to about thirteen quadrillion percent per year [2]

cache layers and mesh network relays. This will provide caching of data and relaying of data between ground-based mesh networks.

2.1.3 Ground Stations

Ground stations will provide the satellite *uplink/downlink* operations. These stations will be responsible for ground-based caching, the running of a nexus daemon, and the defining of a route to relay data to the addressed endpoint.

2.2 Software

There are many types of software applications that are integral parts of the functionality and efficiency of Nexus. The software systems are constantly being developed and improved upon as Nexus continues to mature.

- **Daemon**

Nexus operates on a lower-level software application called the "*Nexus Daemon*". Instances of this software application communicate with one another, forming a peer-to-peer network. They exchange data in the form of transactions and secure them into a distributed database called a blockchain.

- **Wallet**

A command line and graphical Qt version of the Nexus wallet is currently available for download [5] [9]. A new version of the Nexus wallet will be a higher-level graphical application written in the Electron Framework. This will allow access to the functions of the "*Nexus Daemon*" through a HTML/JS interface with native Windows, Linux, and Mac OS X installers.⁵

- **Library**

The lower-level library includes three parts, namely Crypto, Database, and Protocol. They form a lower-level set of programming base templates that can be used to create more complex class structures on top of them.

⁵This is under active development at the time of this writing.

3 Specifications

This section provides details on the specifications of the main software component of Nexus, the "*Nexus Daemon*". This software component is the foundation of the Nexus Network and takes into account Precise Emission, Mining, Trust, and other components of security and efficiency.

3.1 Hashing

Hashing is a critical part of any cryptocurrency. The recent SHA-1 collision computation by Google underscores the need for more secure hashes [19]. One of the innovations of Nexus is the use of newer hashing functions with the goal of enhanced security.

3.1.1 SHA-2

SHA-256 is a member of the SHA-2 set of cryptographic hash functions.⁶ It was designed by the National Security Agency (NSA) and published in 2001 [15]. SHA-256 is used in Bitcoin mining and in the creation of Bitcoin addresses [53].

3.1.2 SHA-3

Nexus uses a newer, more secure hashing algorithm than that of Bitcoin. The SHA-3 [54] standard was the result of a competition [20] with the goal of producing an alternative to SHA-2. This competition was organized by the National Institute of Standards and Technology (NIST). The winner of this competition was selected in 2012. The new SHA-3 standard algorithm is a subset of the cryptographic primitive family, Keccak [55].

3.1.3 Skein

The Skein algorithm was the runner up in the NIST hash function competition [56]. It is also used in Nexus, in combination with SHA-3. The advantage of this approach is greater diversity in the secure hashing functions used in Nexus.

⁶SHA stands for Secure Hashing Algorithm.

3.1.4 Skein-Keccak

Nexus hashing is built from two secure hashing algorithms: Skein and Keccak [17]. These two algorithms are combined to form a single SK-1024 (Skein-Keccak 1024 bit) hash. There are three types of output lengths in Nexus hashing: SK-256, SK-512, and SK-1024. Public keys are hashed with SK-256 to secure them from public knowledge until spent. Transactions are hashed with SK-512 while SK-1024 is used for the proof-of-work hash.

3.1.5 Comparison of 256 bit and 1024 bit

The following example illustrates the difference in size between a Nexus block hash and a Bitcoin block hash:

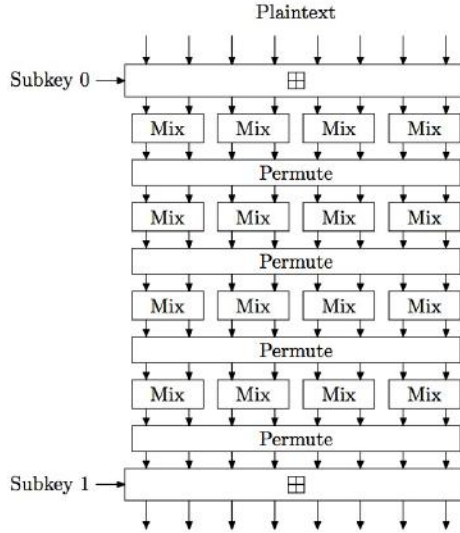
- Bitcoin Hash (256 bit)

```
00000000000000000478710bb73175549d34893a375
454df1af122c26a453d9b
```

- Nexus Hash (1024 bit)

```
0000000001370e3764cffad92091c99b5beaf85f6fc
edae66e77be9de6f0ce6e3d8b1da4b6581d35f3ff6c
f359b10ab85c3b226f41cf864c979e8492f854c56d3
0e329ffc012c338caa7f3c6197137afb1637adc0b2f
22270990d0034c0ea0eae306ec28b7a565a1459896d
69a1c20f9f63af6c5fd672d76c6c8934e8363a21
```

Figure 1: Four of the 72 rounds of the Threefish-512 block cipher used in Skein [16].



3.2 Emission

In Bitcoin, a fixed amount of BTC is available as a reward for miners in every block. This amount halves every four years, thereby reducing Bitcoin's inflation. However, this sudden change in the block reward is a shock to the market. Miners spend large sums of money on equipment and personnel. When the block reward halves, their profits are cut in half overnight.⁷ Such uncertainty could possibly have a negative effect on network security [24]. Nexus improves upon this model by adjusting the reward with every block. Using the equations for exponential decay (*with carefully chosen constant k*), (e^{-kt}) , a deposit is made into reserves every minute. The reserve determines the available reward for miners.

The supply is locked to time and not the block production rate. Inconsistent block times have no effect on the exact supply. This allows the projected supply to be accurately calculated at any second past the network time lock.

3.2.1 Reserves

A traditional water reservoir holds water that can be drawn upon by a town. The total amount of water the town can draw is limited based on how much is in the reservoir. In a similar way, the Nexus reserve system controls how much NXS is available to miners at a given time.

There are three reserves. The amount of NXS deposited into each reserve is mathematically determined by the *decay equations*.

$$\begin{aligned} V_d &= 1 \cdot e^{-0.00000059 \cdot T_m} + 0.032 \\ V_a &= 10 \cdot e^{-0.00000055 \cdot T_m} + 1 \\ V_m &= 50 \cdot e^{-0.0000011 \cdot T_m} + 1 \end{aligned} \tag{1}$$

Where T_m is the time in minutes and V_d , V_a , V_m are the reserve deposit amounts for miner, ambassador, and developer reserves.

⁷Theoretically because this reduction in profits can be foreseen, miners can prepare for it ahead of time. Realistically, it's difficult for miners to account for this in a fast-changing system.

3.2.2 Rewards

The rewards are calculated based on the reserve value. This prevents surplus emission beyond the target level. These three equations describe the intervals in which the block reward V_b changes based on reserve values V_m at T_m by compounding the T_m value from equations 1.

$$V_b = \begin{cases} \frac{T_a}{60} \cdot V_r, & T_m \leq 2.5 \\ 2.5 \cdot V_r, & 2.5 < T_m < 20 \\ 3.0 \cdot V_r, & T_m \geq 20 \end{cases} \quad (2)$$

Where T_a is the actual time, T_o is the offset time, and T_t is the target time.

3.2.3 Minting

Peer-to-peer networks, such as Bitcoin and Nexus, require the support of many nodes around the world. If there aren't enough nodes, network stability, decentralization, speed, and security suffer. Bitcoin suffers from a tragedy of the commons⁸ issue wherein everyone wants more people to run the peer-to-peer wallet, but there is little incentive to do so. Nexus solves this problem by rewarding people with newly minted coins for holding Nexus and keeping their wallet up and running 24/7. To put it simply, if someone installs the Nexus wallet on their computer and deposits enough NXS, then they will occasionally find a block and earn extra NXS.⁹

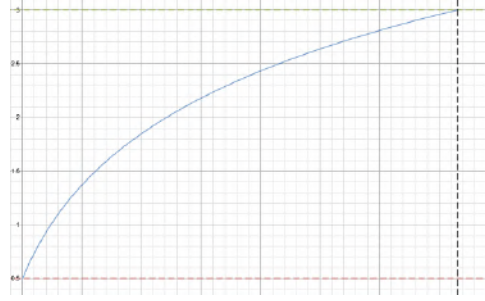


Figure 2: Interest Rate Graph.

This minting system operates to give people larger rewards for greater contribution to the network. As one produces blocks by using this method in a

⁸The tragedy of the commons is an economic problem in which every individual tries to reap the greatest benefit from a given resource. As the demand for the resource overwhelms the supply, every individual who consumes an additional unit directly harms others who can no longer enjoy the benefits [35].

⁹This is a way to support the network and earn Nexus without costly and difficult-to-operate mining hardware and software.

timely manner, one's trust grows. With a higher trust score comes a higher minting rate. The minting rate R_m ranges from 0.5 % - 3 %.

$$R_m = \frac{0.025 \cdot \ln(\frac{9 \cdot a_t}{31449600}) + 1}{\ln(10)} + 0.05 \quad (3)$$

Where a_t is the age of your trust key (the number seconds since the trust key's genesis transaction).

3.3 Block Validation

There are three ways to produce a valid Nexus block and mint new NXS. There are two proof-of-work channels and one proof-of-holdings channel. The proof-of-work channels are the Prime Channel and the Hashing Channel. In the Prime Channel, miners search for Dense Prime Clusters of 308 digits in size. In the hash channel, standard Hashcash [18] style work is computed using the SK-1024 hashing algorithm. The two proof-of-work channels prevent each other from producing too many blocks in a row, thus forcing a 51% attacker across both channels.¹⁰

3.3.1 Dense Prime Clusters

The work done by miners in the Prime channel is a search for dense prime clusters [42].¹¹ Finding these dense prime clusters is a trial-and-error process. Miners must try many numbers to successfully find one that is the beginning of a dense prime cluster [41, 36].

The count of prime numbers in a dense prime cluster is called its chain length.¹² A dense prime cluster with a longer chain length is more difficult to find than one with a shorter chain length. The first prime number in the chain is required to be higher than the block hash and less than the block hash plus 2^{64} .¹³ If the first prime in the cluster fits these criteria, it

¹⁰Reserves between Prime and Hash are split evenly at 50 %

¹¹The numbers found in these searches are actually probable primes [38]. They pass the Fermat primality test [39] at base 2.

¹²The "chain" here should not be confused with the chain in blockchain.

¹³The block hash can't be determined a priori for future blocks because it's based on previous block information. Therefore, a miner must start their prime cluster search over again after each new block is found.

is considered a valid solution.

One benefit to searching for dense prime clusters is that it is thought to be more resistant to GPU, FPGA, and ASIC mining than hashing. Another is that the data produced by the miner is useful for mathematical research into prime numbers [40] [37]. The applications of prime number research may extend beyond mathematics and into quantum physics [43]. This is one of the ways that Nexus provides value back to the scientific community and the world.

3.3.2 Hashing

The hashing channel uses a *Hashcash* [18] style proof-of-work. Miners run code [6, 7] on GPUs in an attempt to find a hash that meets a given difficulty. If they are lucky, they will find a hash with at least a certain number of leading 0 bits. This means that the hash is preceded by a number of 0's and is a smaller integer. This is called a "partial collision". This is similar to the proof-of-work scheme that Bitcoin uses. Bitcoin uses SHA-256 while Nexus uses the newer SHA-3 in combination with Skein.

3.3.3 Holdings

Proof-of-Holdings (*POH*) provides a third channel of security. An attacker would need to gain 51 percent of the NXS supply to attack this channel in conjunction with the hash and prime channels. The incentive for this proof system is newly minted coins which are rewarded to participants for actively "holding" their coins. This means the network incentivizes users to contribute to the security of the system. This provides a natural growth in the coin supply over time that will be highly beneficial to the network, economy, and users.

Unlike current Central Bank models, this new supply of coins goes directly into the users hands rather than being filtered through a fractional reserve system. Furthermore, these newly minted coins have zero debt associated with their issuance and, therefore, never need to be paid back to the system with associated interest, as is the case with many current fiat currencies. The minting rate was determined to be a variable rate between .5% and 3% to provide a small natural growth to the coin supply allowing for increased economic opportunity.

3.4 Difficulty

The difficulty of finding a block is adjusted with every new block. The Nexus difficulty algorithm combines weighted averages for the last n blocks. A weighted average time, T_a is calculated as follows:

$$T_a = \frac{\sum_{i=1}^n w \cdot i [T_b(H-n+i) - T_b(H-n+i-1)]}{n} \quad (4)$$

Where H is the current block height, T_b is the block time stamp at a given height, n is the blockchain depth, and w is a weight constant (currently set to 3).

Mod_d is the factor used to modify the difficulty

$$Mod_d = \begin{cases} [1 - (Min_d \cdot T_o)] \cdot T_t, & \text{if } T_a \geq T_t \\ [1 + (Max_d \cdot T_o)] \cdot T_t, & \text{otherwise} \end{cases} \quad (5)$$

Where T_t is the target time, T_o is the offset time, Min_d is the minimum difficulty decrease and Max_d is the maximum difficulty increase.

It's a vice to trust everyone, and
equally a vice to trust no one.

Seneca

3.5 Trust

Trust is a core component of Nexus. Nodes which have a vested interest in and are acting to benefit the whole network by participating honestly and consistently are considered more trustworthy. Currently, trust is earned by holding Nexus in a wallet and producing valid blocks on a regular basis. This earned trust is recorded in the Nexus blockchain and is associated with a trust key.

Future areas of research and development in Nexus are focusing on using the concept of trust in many ways. Using trust, a new security model can be developed around time. The strength of the Nexus economy and its reliability will be reinforced by promoting truthfulness between the voluntary interactions with individuals and groups of individuals.

3.5.1 Weight

Weight governs the speed in which one can search for new trust blocks. It comes in the form of two different weight variables: Block Weight (W_b) and Trust Weight (W_t).

$$W_t = \text{Min}(17.5, \frac{16.5 \cdot \ln(\frac{2 \cdot a_t}{2419200}) + 1}{\ln(3)} + 1.0) \quad (6)$$

$$W_b = \text{Min}(20.0, \frac{19.0 \cdot \ln(\frac{2 \cdot a_b}{86400}) + 1}{\ln(3)} + 0.05) \quad (7)$$

Where a_t is the trust age and a_b is the block age.

3.5.2 Threshold

A system has been developed to allow an energy-efficient time-based trust system. This is regulated by the Energy Efficiency Threshold E_t .

$$E_t = \frac{100 \cdot T_a}{N_{once}} \quad (8)$$

The Required Threshold R_t is

$$R_t = \frac{(50 - W_t - W_b) \cdot 1000}{C} \quad (9)$$

Where C is the total NXS in a trust transaction.

3.5.3 Genesis

The genesis transaction is the first transaction of a trust key. This is required to act as the root of the trust key's age in order to gain a reference on its current weight and minting rate. The hash of this genesis transaction can therefore be used as an input in future transactions to verify that a trust block is linked to a corresponding genesis transaction.

The following equation describes the genesis weight required to get a high enough threshold to achieve the creation of a genesis transaction and corresponding block¹⁴

$$W_g = \text{Min}(17.5, \frac{16.5 \cdot \ln(\frac{2 \cdot a_c}{7257600}) + 1}{\ln(3)} + 1.0) \quad (10)$$

Where a_c is the coin age of the coins which are being used.

3.5.4 Intervals

Trust blocks cannot be created from the same trust key unless the interval or number of blocks between their last trust block exceeds $I_t \geq 6$.

3.6 Clock Drift

Clock drift refers to several related phenomena where a clock does not run at exactly the same rate as a reference clock [8]. This is usually resolved by connecting to a central server and/or atomic clock. Nexus combats this with a peer-to-peer time-keeping system that keeps all clocks on the network synchronized to the unified time seed.

3.7 Security

When the clocks are synchronized, a higher level of security occurs with regards to the timestamps. This is because Bitcoin and other cryptocurrencies generally allow up to 2 hours in the future for clock drift, which means that

¹⁴Genesis transaction weight does not include block weight.

blocks can be created up to 2 hours from the *timestamp*, thereby leaving potential attack vectors. Nexus combats this synchronization not with median time, as Bitcoin uses, but rather with a Unified Time system that operates on the protocol level keeping all Nexus clocks synchronized to the second.

3.8 Time-Locks

Because clocks in the Nexus network are synchronized, new rules can be activated in the protocol based on time stamps rather than block numbers. This allows network participants to more accurately activate consensus updates.

3.9 Checkpoints

Automated decentralized checkpoints are created every hour. A checkpoint prevents any block that was not rooted from the last hardened checkpoint to be invalid. This prevents an attacker from producing an alternative blockchain prior to the last checkpoint time.

I think I can safely say that
nobody understands quantum
mechanics.

*Professor Richard Feynman, 1965
Physics Nobel Laureate [21]*

4 Post-Quantum Considerations

4.1 Grover's Algorithm

Grover's algorithm is a quantum algorithm which was devised by Lov Grover at Bell Labs. The summary in Grover's 1996 paper provides a helpful description: "Imagine a phone directory containing N names arranged in completely random order. In order to find someone's phone number with a probability of one half, any classical algorithm... will need to look at a minimum of $N/2$ names. Quantum mechanical systems can be in a superposition of states and simultaneously examine multiple names ... As a result, the desired phone number can be obtained in only $O(\sqrt{N})$ steps [62]."

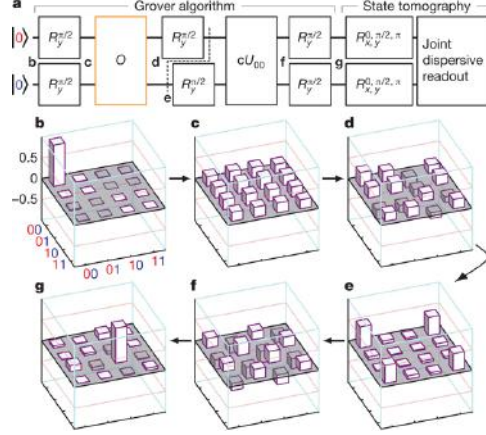


Figure 3: Grover's Algorithm on Two Qubits

Given the output of a black box function, it can be used to determine¹⁵ the input. This implies that most one-way cryptographic hash functions are susceptible to this algorithm. Indeed, Grover's algorithm could brute-force a 256-bit key in roughly 2^{128} iterations.

The algorithm proceeds to call $G \left[\frac{\pi}{4} \cdot 2^{\frac{k}{2}} \right]$ times in the verification of the subroutines. The largest overhead, though, in Grover's Algorithm is the cost of error detection that must be done classically to ensure the accuracy of the qubits and the two subroutines of Grover Iteration.

The first subroutine of G is attempting to assert $g : \{0, 1\}^k \rightarrow \{1, 0\}$ maps X to 1 only if $f(x) = y$. The next subroutine is called the "*Diffusion Operator*", and it implements the transformation of g to increase the probability that $f(x) = y$.

As illustrated in Table 1, Grover's Algorithm results in a nearly 50% reduction to the security provided by one-way hashing functions against brute-

¹⁵In a probabilistic manner.

Table 1: Resource Comparison for Grover Search of SHA-256 and SHA3-256 [23, p. 18]

		SHA-256	SHA3-256
Grover	T-count	$1.27 \cdot 10^{44}$	$2.71 \cdot 10^{44}$
	T-depth	$3.76 \cdot 10^{43}$	$2.31 \cdot 10^{41}$
	Logical qubits	2402	3200
	Physical qubits	$1.39 \cdot 10^7$	$1.94 \cdot 10^7$
Distilleries	Qubits per Distillery	3600	3600
	Total Distilleries	1	294
	Code Distilleries	{33, 13, 7}	{33, 13, 7}
	Physical qubits	$5.54 \cdot 10^5$	$1.63 \cdot 10^8$
Total	Logical qubits	$2^{12.6}$	2^{20}
	Code Cycles	$2^{153.8}$	$2^{146.5}$
	Total Cost	$2^{166.4}$	$2^{166.5}$

force attacks. This implies that a hash, which has twice as many bits, should be used to achieve the same level of security against brute-force attacks.

4.2 Elliptic Curve Cryptography

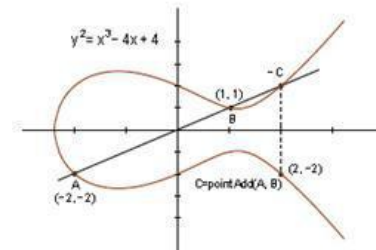
Elliptic Curve Cryptography, in terms of classical computing, retains high security standards with smaller key sizes compared to RSA [58]. The following equation can be used to represent an elliptic curve:

$$y^2 = x^3 + ax + b \quad (11)$$

4.3 Curve Groups and Fields

In Nexus, the elliptic curve domain parameters are based on *sect571r1* [12] as defined in the “Standards for Efficient Cryptography 2: Recommended Elliptic Curve Domain Parameters” and they are defined over a binary field \mathbb{F}_{2^m} . The domain parameters that are used in most other digital currencies are based on *secp256k1* [13]. These parameters are associated with a Kolbitz curve and are defined over a prime

Figure 4: Illustration of an Elliptic Curve



field \mathbb{F}_p .

4.4 Private Keys

A private key is a number that should only be known to the owner of the coins in a given address. To produce a secure private key, it's necessary to start with a number that is as close to truly random as possible.¹⁶ If anyone is able to determine what the private key is, they can move the coins to another address. This is why private key security is so important. You don't want anyone else to find out what your 'secret number' is, and you don't want them to be able to guess it or determine it with a complex algorithm based on public information. Both Bitcoin and Nexus use large numbers so that there is almost no chance that anyone else will generate the same random number, and it is impossible for anyone to try all of the numbers.¹⁷ Bitcoin keys are 256 bits in length, while Nexus keys are more than twice as long at 571 bits.

Bitcoin Private Key (256 bit)

5Kb8kLf9zgWQnogidDA76MzPL6TsZZY36hWXMssSzNydYXYB9KF

Nexus Private Key (571 bit)

6Wuiv513R18o5cRpwNSCfT7xs9tniHHN5Lb3AMs58vkVxsQdL4atHTF
Vt5TNT9himnCMmnbjbCPxgxhSTDE5iAzCZ3LhJFm7L9rCFroYoqz

4.5 Public Keys

The public key is derived from the private key using elliptic curve cryptography. It's easy to derive a public key from a private key, but not a private key from a public key. However, there is concern that, in the future, this may be possible with quantum computers. Fortunately, modern cryptocurrencies, including Nexus and Bitcoin, do not require users to share even their public key. When you request a payment in Nexus from someone, you first get a *Nexus address* from your wallet. This address is not your public key. It's

¹⁶This is handled by the Nexus wallet software - it generates private keys and stores them.

¹⁷"How many numbers? For every grain of sand on Earth, create a new Earth. There are 26 billion unique Bitcoin addresses for each grain of sand on each of those Earths." [52] Because the keys in Nexus are longer, there are astronomically more possible Nexus addresses.

called a public key hash, or *PKH*. As the name implies, it's created by taking a hash of the public key. This means that an attacker who wants to figure out your private key first has to determine your public key from the *PKH*. Fortunately, this is an intractable problem. Current research indicates this may take even quantum computers on the order of a hundred billion years [48, 49]. The public key associated with a *PKH* is not revealed until the coins are spent [26]. Therefore, one can achieve a high level of quantum attack resistance simply by not re-using addresses.

Now let's consider the question: If an adversary did know your public key, how hard would it be for them to determine the all-important private key? For the answer to this question, we look to the work of Peter Shor.

4.6 Shor's Algorithm

In 1994, Peter Shor devised a method which could be used to solve the Integer Factorization Problem *IFP* and the Discrete Logarithm Problem *DLP* in polynomial time on a quantum computer [44]. This was an important achievement because these problems have no classical polynomial time solution. This means that, on a classical computer, they can't be solved in any amount of time which can be represented by n^k - for example n^2 , n^3 , etc.¹⁸

Because of this, they are used in cryptographic systems.

The Elliptic Curve Discrete Logarithm Problem (*ECDLP*) is a special case of the *DLP* for elliptic curves. This is a more difficult problem to solve classically than the *DLP*. [45] This is the type of problem that needs to be solved in order to determine the private key from the public key for cryptocurrencies, such as Bitcoin and Nexus.

4.7 Zalka, Proos and Kaye

Christof Zalka, along with John Proos and Phillip Kaye, have extended Shor's work by designing algorithms optimized for solving the *ECDLP*. The result is the Proos-Zalka and Kaye-Zalka algorithms.

¹⁸In layman's terms, this means that finding a solution is infeasible as long as a large enough number is used.

4.8 Proos-Zalka Algorithm

The Proos-Zalka algorithm was specifically designed to solve the *ECDLP* over a prime field \mathbb{F}_p on a quantum computer. This is an attack on elliptic curves over a finite field. The qubit requirement for the breaking of the ECDLP over a prime field of n bits is as follows [45]

$$5 \cdot n + 8\sqrt{n} + 4 \log_2 n + 10 \approx 6n \quad (12)$$

4.9 Kaye-Zalka Algorithm

The Kaye-Zalka revision addresses curves over the binary field \mathbb{F}_{2^m} . This specific field takes advantage of binary computation to bring quicker verification on larger keys. The equation modeling the qubits required to break a key of \mathbb{F}_{2^m} is as follows [46]

$$2m + 7 \cdot \log m + 7 + H \approx 2m \quad (13)$$

Where H is related to the halting counter and is of order $\log(m)$.

4.10 The Benefits of Larger Keys

”Key length defines the upper-bound on an algorithm’s security since the security of all algorithms can be violated by brute force attacks [58].”

As of 2015, a minimum key length of 224 bits is recommended for elliptic curve algorithms [60]. Bitcoin keys are $256 - 224 = 32$ bits longer than this requirement while Nexus keys are $571 - 224 = 347$ bits longer. According to the National Security Agency “Elliptic Curve Public Key Cryptography using the 256-bit prime modulus elliptic curve as specified in FIPS-186-2 and SHA-256 are appropriate for protecting classified information up to the SECRET level. Use of the 384-bit prime modulus elliptic curve and SHA-384 are necessary for the protection of TOP SECRET information [59].”

Brute Force Resistance

The Large Bitcoin Collider [57] is a project that attempts to brute force-attack Bitcoin. Participants in this project generate as many Bitcoin public addresses as possible by first choosing a random number in a given range. Rarely, they happen to generate a public address that happens to contain Bitcoins and the Bitcoins can be stolen since they know what the private

key is.¹⁹

Key length defines the upper-bound on an algorithm’s security [58] against brute-force attacks. Nexus uses significantly larger 571-bit keys than Bitcoin’s 256-bit keys and is thus postulated to be more resistant to these attacks.

In any case, Rico - the pseudonymous lead of the LBC states: ”Finding a P2PKH²⁰-collision [one cryptographic method of creating bitcoin addresses] would probably mean the end of P2PKH but not bitcoin,” ... ”Bitcoin would evolve with new address types. Most certainly it wouldn’t ’die’ because of this.” [57] This highlights one of the ways that Nexus is providing value back to the Bitcoin ecosystem. By using different elliptic curve parameters and different hashing algorithms, Nexus is paving the way for possible future enhancements to Bitcoin. Instead of merely researching or discussing alternatives, Nexus is proving them on a live blockchain.

Longer Solution Time

It will take more time for a quantum computer to solve the *ECDLP* if the key is larger. The run times are predicted to be of order $O(n^2)$ [45, 46]. This means that a key which is twice as long will take approximately four times as long to find with a quantum computer.

Table 2: Qubits and Time required to break each key size for \mathbb{F}_p [25]

Quantum IFP			Quantum ECDLP			Classical
λ	Qubits λ	Time $4 \cdot \lambda^3$	λ	Qubits $7 \cdot \lambda$	Time $360 \cdot \lambda^3$	Time
512	1024	$0.54 \cdot 10^9$	110	700	$0.50 \cdot 10^9$	c
1024	2048	$4.30 \cdot 10^9$	163	1141	$1.60 \cdot 10^9$	$c \cdot 10^8$
2048	4096	$34 \cdot 10^9$	224	1568	$4.0 \cdot 10^9$	$c \cdot 10^{17}$
3072	6144	$120 \cdot 10^9$	256	1792	$6.0 \cdot 10^9$	$c \cdot 10^{22}$
15360	30720	$1.5 \cdot 10^{13}$	512	3584	$50 \cdot 10^9$	$c \cdot 10^{60}$

Where λ is the input length in bits.

¹⁹There are a couple of ways to mitigate the risk of such an attack on your Bitcoins. First, don’t keep too many coins in one address. Second, use multisig.

²⁰Pay to Public Key Hash[61]

4.11 Side Channel Attacks on secp256k1

As previously mentioned, Bitcoin uses the 256 bit *secp256k1* elliptic curve domain parameters as defined in the Standards for Efficient Cryptography. Under special circumstances, a Bitcoin private key can be determined by another process on the same classical computer in as few as 200 signatures [50].²¹ With quantum computing on the horizon, and the fact that ECC already leaks private keys classically with side channel attacks, serious considerations must be made on the logic of any use of digital signature algorithms to prove ownership of any tokens. This is the focus of ongoing research and development in Nexus.

4.12 Key Accommodations in Nexus

Nexus currently supports key sizes as large as 571 bits, specifically sect571r1. In order to offer more choice and to take advantage of the larger number of qbits required to crack curves over prime fields, we will also implement keys using different curves.

The choice of elliptic curve parameters is subtle; care must be taken to avoid security pitfalls. Several parameter choices have been developed, as described on the SafeCurves website [47]. We plan to add support for multiple curves to Nexus in the future, giving people the choice of what curve to use and the ability to use multisig with multiple curves.

4.13 Post-Quantum Cryptography

Since the newly emerging quantum computer era is almost upon us, and many cryptographers are working on new quantum encryption methods, Nexus has chosen to use key suites and high-bit keys to provide quantum resistance while the post-quantum industry matures. The projected time before any practical quantum computers that could do any damage is around five to ten years. By doubling Nexus key size, the required run time is quadrupled; this provides more time to carefully choose a post quantum cryptographic method. This is projected to be within the next few years as the development of post-quantum cryptography is observed and studied more thoroughly.

²¹This is called a "side channel" attack.

5 Conclusion

With modern hashing, upgraded private keys, multiple block validation methods, decentralized checkpointing, time synchronization, decentralized trust, variable block reward, time locked emission, decentralized minting, lower level library, quantum considerations, ground based mesh networks, and low earth orbit satellite constellations Nexus is one of the most technologically advanced frameworks on the planet. Furthermore Nexus also represents a vision for a better future for all mankind aligned with the principles of life, liberty and the pursuit of happiness.

We now have an opportunity to step away from existing systems by simply changing our focus. We can choose to look away from the systems of the past and focus our energy on the systems of the future. Through the Nexus framework, users now have the tools needed to change the focus and connect through a mathematically and cryptographically validated network. Nexus exists as a publicly available, free-to-use, peer-to-peer network for people to connect and improve the efficiency and quality of their lives. Peer-to-Peer technologies have the capability to help us reshape our world and Nexus represents an important step forward in this process. The noun "nexus" is defined as: a connection or series of connections linking two or more things. Nexus is an idea of connection and the technology to make this possible. It is through this connection that people will have the opportunity to act together in accord with one another, and pursue a future that is filled with wisdom, prosperity and joy. Welcome to Nexus!

A Current Research and Development

There are many areas of research currently under development for prospective implementation into the Nexus framework. These include but are not limited to: scalability solutions, contracting engines, the TAO update series (Tritium, Amine, Obsidian), multi-level locking, lower level database enhancements, post-quantum cryptography, governance systems, protocol level checks and balances and social organization models.

Action without Vision is a
Daydream, Vision without
Action is a Nightmare.

B Vision

Vision is one's ability to think about or plan the future with wisdom. Wisdom is the quality of having experience, knowledge, and good judgment. In this case, vision is coupled with wisdom, which is a direct result of experience and, therefore, knowledge. This means that vision is attainable if one is willing to learn from the experience of the world. Vision can be understood at a greater depth by applying the following to conduct:

1. **Capable** of verifying and/or understanding without premature conclusion
2. **Discipline** to see *what is* - unaltered by definitions and belief systems
3. **Knowledge** gained through the study of reality, society, and the work of others
4. **Accordance** with the laws of nature, virtue in accordance with the laws of the self
5. **Principle** formed through the understanding of this accordance

C Philosophy

Philosophy is the study of the fundamental nature of knowledge, reality, and existence - *as it is* - with intent to understand *what it is*. Following

will include a short list of philosophies forming a foundation for vision and principle to integrate into greater virtue, reason, and success in the form of happiness being the ultimate value in which each individual seeks.

I must not fear.
Fear is the mind-killer.
Fear is the little-death that brings total obliteration.
I will face my fear.
I will permit it to pass over me and through me.
And when it has gone past I will turn the inner eye to see its path.
Where the fear has gone there will be nothing.
Only I will remain.

22

C.1 Nicomachean Ethics

Aristotle was an ancient Greek philosopher and scientist [31]. Aristotle believed that virtue was essential in achieving the ultimate goal: happiness.

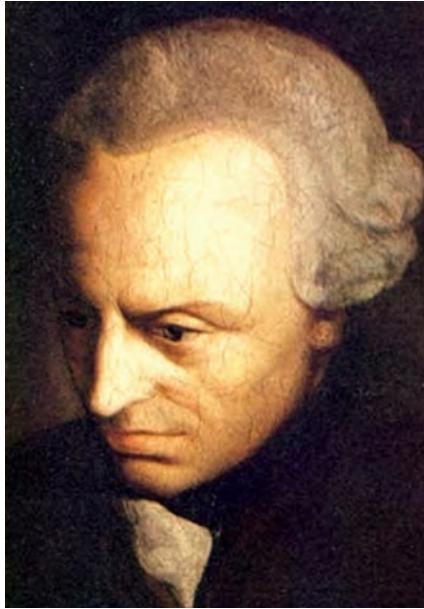
As a portion of the philosophies described in his works on Nicomachean Ethics, an idea was formed under the name the "*golden mean*" which described a world of excess and deficiency. This philosophy described the evils of the world - or oppositions to the growth of life - to be either excess or deficiency. The golden mean is described as the quality of having neither excess or deficiency but rather a "golden mean" between the two extremes.



²²Bene Gesserit Litany Against Fear - From Frank Herbert's Dune Book Series

C.2 Kingdom of Ends

Immanuel Kant was born ahead of his time on the 22nd of April, 1724 in Berlin, Germany [32]. He had many philosophies that are still studied to this day. One of his more notable works was called the *Kingdom of Ends*. He describes a hypothetical existence where individuals act entirely rationally, and with reason. He defines these people as ones capable of proper conduct. He proposed that when those that were capable were able to live under a common law of laws that were of the utmost importance and necessity, that a more harmonious and *moral* society could form as a *Kingdom of Ends*.



These common laws could be considered reference points for the value of actions in a Kingdom of Ends, to where its correlation with universal law provides the greatest value to those of the Kingdom of Ends. His second formulation showed that individuals that live in accordance with the principle to treat ones fellowmen as end in themselves, were capable of greater virtue, and therefore, joy. This describes an idea and philosophy of acting in accordance and harmony with one's people as a kingdom of ends, rather than each individual seeking one another as means to their own ends.

"People can only belong to the Kingdom of Ends when they become subject to these universal laws. Such rational beings must regard themselves simultaneously as sovereign when making laws, and as subject when obeying them. Morality, therefore, is acting out of reverence for all universal laws which make the Kingdom of Ends possible. In a true Kingdom of Ends, acting virtuously will be rewarded with happiness." ²³

²³Excerpt quoted from https://en.wikipedia.org/wiki/Kingdom_of_Ends

C.3 The Tao

In ancient China, the keeper of the Imperial Library, Lao Tzu, was famous for his wisdom. Perceiving the growing corruption of the government, he left for the countryside. On his way, the guard at the city gates asked Lao Tzu to write out the essence of his understanding to benefit future generations. Lao Tzu wrote the Tao Te Ching, left, and was never heard of again [33].

[34] Chapter 1 of the Tao Te Ching: 章

The "Tao" is too great to be described
by the name "Tao". If it could be named
so simply, it would not be the eternal Tao.

Heaven and Earth began
from the nameless (Tao), but the multitudes
of things around us were created by names.

We desire to understand the world
by giving names to the things we see, but these
things are only the effects of something subtle.

When
we see beyond the desire to use names, we
can sense the nameless cause of these effects.

The cause
and the effects are aspects of the same, one
thing. They are both mysterious and profound.

At their most mysterious and profound
point lies the "Gate of the Great Truth".

道可道

非常道

名可名

非常名。

無, 名天地之始

有, 名萬物之母。

故常無欲以觀其妙

常有欲以觀其微。

此兩者

同出而異名

同謂之玄。

玄之又玄

衆妙之門。

People must have righteous
principles in the first, and then
they will not fail to perform
virtuous actions.

Martin Luther

D Principles

Principles are the extensions of philosophies that derive frameworks of thought and act as guidelines of proper conduct between ourselves and others.

D.0.1 Individual

1. **Evaluate** as a means to greater **Knowledge**
2. **Happiness** as a result of **Virtue**
3. **Respect** as a result of **Depth**
4. **Freedom** as the truest **Expression**

D.0.2 Collective

1. **Objective** with Receptivity, **Honest** with Communication
2. **Respectful** in Conduct, **Understanding** in Conflict
3. **Honor** to spoken Word, **Harmony** to Action

E How We Make Change

The cells of our body work together to provide the capacity for life. Similarly, we can compare the cells of our planet to each individual. If we understand the benefits of cooperation, challenges can be resolved thoroughly and quickly without unnecessary difficulties. This is how we make change; we work together to resolve challenges with viable solutions. This is the most efficient and effective way to bring change in the direction of our greatest preferences.

The community is the very foundation of an economy. An economy is only as strong as its foundation. When people lose faith in an economy, the base of the economy will collapse and the value of its system will fall with it. The Nexus community is already very resilient to the stress of markets. The community is a positive and inclusive group of people from across the world who are all aiming towards the same goals of transparency, prosperity, and freedom.

Nexus aims to build a strong community based on a savings culture and charity. The savings culture has been long lost but it is the best insurance policy for any uncertain times that may lie ahead. This helps the community hedge itself against high risk and volatile markets. The idea is that your community member is your neighbor. If your neighbor does well, your local economy will prosper as well.

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